by EFLS and other techniques.

Jennings<sup>2</sup> had alluded to a disadvantage of EFLS; namely, that the polymer size must be comparable to the wavelength of light. This can be overcome by using low-angle X-ray (LAXS) and neutron scattering (LANS) techniques in the presence of an electric field. The theory presented here would apply in the case of LAXS and LANS in an electric field, except that the polarizability  $\alpha$  would be replaced by electron density and scattering length, respectively.

#### Conclusions

Electric field induced light scattering is a technique that is potentially useful in several areas of polymer characterization. By doing two EFLS experiments on the same polymer sample, one can separate out the two effects contributing to EFLS, namely, the fluctuation term which comes about from polymer flexibility and the orientation term. The first term is important for determining the degree of polymer flexibility and is useful for characterizing liquid-crystal polymers. For example, it can be used to distinguish between rods, disks, and semiflexible polymers. The second term will be sensitive to the details of polymer structure and can complement other methods for characterizing polymer, such as end-to-end distances, dipole

moments, and Kerr effect. When EFLS is performed in the small-angle scattering regime, the theoretical expression for it can be evaluated exactly by using the RIS model.<sup>9</sup> In that case, there can be a simple direct comparison between experiment and theory.

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# Dynamic Light Scattering Studies of Polymer Solutions. 6. Polyisoprenes in a θ-Solvent, 1,4-Dioxane

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ABSTRACT: The dynamic properties of polyisoprenes in 1,4-dioxane at 34.7 °C (the  $\Theta$ -temperature) have been studied by homodyne photon correlation spectroscopy. The infinite dilution characteristics, the translational diffusion coefficient  $D_0$ , and the effective decay rate (the first cumulant)  $(\Gamma_{\bf e})_{c\to 0}$ , have been analyzed as functions of the scattering vector  $\bf q$ . It has been found that isoprene chains in the unperturbed state are fairly well described by the nondraining Gaussian model with nonpreaveraged Oseen hydrodynamic interaction. However, it has been revealed that some 10% and some 20% differences of  $D_0$  and  $(\Gamma_{\bf e})_{c\to 0}$ , respectively, exist between experiments and theories. The former difference might be explainable in terms of the internal friction of chains, which has recently been introduced by Fixman. The concentration dependence of the translational diffusion coefficient is also discussed in some detail.

#### Introduction

At the  $\Theta$ -temperature where the excluded volume effect vanishes, dynamic light scattering by dilute polymer solutions provides precise information on the nature of the hydrodynamic interaction between chain segments. Experimental studies<sup>1-3</sup> so far made for an oridinary  $\Theta$ -solution, polystyrene (PS) in cyclohexane, trans-decalin, and so on, have shown some puzzling results, for example, the superiority of the preaveraged (PA) form of the Oseen hydrodynamic interaction to the non-PA form and a 15% or 20% reduction of the translational diffusion coefficient  $D_0$  from the Kirkwood value. These situations have been clearly summarized in the recent review of Stockmayer and Hammouda.<sup>4</sup> Similar results, though not very conclusive, have been obtained also for PS in benzene, a good solvent.<sup>5</sup>

We have recently studied<sup>6</sup> the dynamic behavior of polyisoprene (PIP) in cyclohexane and found that, in the good solvent, PIP chains are well described by the non-

Table I
Characteristics of Polyisoprenes in 1,4-Dioxane at 34.7 °C
(θ-Temperature)

polymer	$10^{-6} M_{\rm w}^{\ a}$	$R_{ m G},10^{-6}~{ m cm}$	microstructure <sup>b</sup>		
			cis-1,4	trans-1,4	3,4
L-14	0.326	(1.91) <sup>c</sup>	73.3	21.9	4.8
L-12	0.568	2.53	67.0	25.3	7.7
L-11	2.44	(5.23)	84.1	11.9	4.0

<sup>a</sup>Measured in cyclohexane at 25 °C.<sup>6</sup> <sup>b</sup>Measured in CDCl<sub>3</sub> at 35 °C by using a 400-MHz <sup>1</sup>H NMR spectrometer.<sup>6</sup> <sup>c</sup>The values in parentheses were estimated from the empirical relation  $R_{\rm G}=3.35 \times 10^{-9} M_{\rm w}^{0.50}$  cm, which was obtained by analyzing the data of Hadjichristidis and Roovers<sup>7</sup> and ours.

draining chain model with the non-PA Oseen tensor and with Domb-Gillis-Wilmers segment distribution. This result which is more reasonable as compared with the previous result for PS seems to be attributed to higher

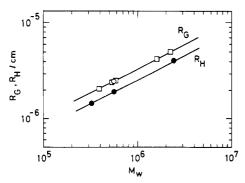


Figure 1. Logarithmic plots of the equivalent hydrodynamic radius  $R_{\rm H}$  and the root-mean-square radius of gyration  $R_{\rm G}$  against the weight-average molecular weight  $M_{\rm w}$  for PIP in 1,4-dioxane at the  $\Theta$ -temperature: circles represent the present data at 34.7 °C; squares the data of Hadjichristidis and Roovers at 34 °C.

chain flexibility of PIP chains.

Thus, in this paper, we reexamine experimentally the dynamic behavior of the unperturbed chain by using another  $\Theta$ -solution, PIP, in 1,4-dioxane at 34.7 °C.

## **Experimental Section**

**Materials.** Three samples, coded as L-14, L-12, and L-11, of previously investigated PIPs<sup>6</sup> were used in this study. Their molecular weights ranged from  $0.326 \times 10^6$  to  $2.44 \times 10^6$ . The homogeneity was verified<sup>6</sup> by the value  $M_{\rm w}/M_{\rm n} < 1.1$ . The characteristics of these samples are summarized in Table I. The root-mean-square radius of gyration of the polymer  $(R_{\rm G})$  in 1,4-dioxane at 34.7 °C was measured only for L-12 in the present work. This value,  $2.53 \times 10^{-6}$  cm, agreed with the data of Hadjichristidis and Roovers<sup>7</sup> as shown in Figure 1. Here an unfilled circle represents our value for L-12 and five squares represent Hadjichristidis and Roovers data at 34 °C. Their samples had the microstructure similar to ours; 70% cis-1,4, 23% trans-1,4, and 7% 3,4. All these data are well fitted by a straight line:

$$R_{\rm G} = 3.35 \times 10^{-9} M_{\rm w}^{0.50 \pm 0.01}$$
 (cm) (1)

We estimated  $R_{\rm G}$  of the remaining two samples, L-14 and L-11, by using eq 1. These values are shown in parentheses in Table I.

1,4-Dioxane (spectrograde, Nakarai Chemicals, Kyoto) was used without further purification. Its purity was checked by measuring the refractive index n for the sodium D line at 25 °C in a Pulfrich refractometer (Shimadzu Seisakusho Co., Kyoto). The result was that  $n^{25}_{\rm D}=1.4199$ , which agreed well with the literature value, 1.42025. We also estimated the refractive index, the density, and the viscosity of 1,4-dioxane at 34.7 °C ( $\theta$ -temperature) as n=1.4197 (488 nm) and 1.4137 (633 nm), d=1.0167 g cm $^{-3}$ , and  $\eta_0=1.019\times 10^{-2}$  g cm $^{-1}$  s $^{-1}$ , respectively, by using the literature values. A bottle containing the solvent was filled with fresh  $N_2$  every time immediately after use and was stored in a desiccator placed in a dark place.

**Preparation of Polymer Solutions.** Polymer solutions of various concentrations were prepared by mixing by weight the solvent and a known concentration solution. They were freed from dust by centrifugation. An antioxidant, about 0.05~w/v % 2,6-di-tert-butyl-p-cresol, was added in the solutions because antioxidant-free solutions showed oxidative degradation during the measurements for a long time, say, 1 h. All the preparative procedures were proceeded in dryboxes under  $N_2$  atmosphere above 32 °C. The solutions thus prepared were stored, under the shade of light, in a box, its temperature being kept above 32 °C.

**Dynamic Light Scattering.** The intensity autocorrelation function  $A(\tau)$  was measured at  $34.7 \pm 0.02$  °C by the same apparatus and procedures described earlier. A vertically polarized single-frequency 488-nm line of argon-ion laser fitted with a space etalon was used as the light source. The scattering angle was fixed at four positions, i.e.,  $30^{\circ}$ ,  $60^{\circ}$ ,  $90^{\circ}$ , and  $120^{\circ}$ .

#### Results and Discussion

**Method of Data Analysis.** At the scattering angles  $\theta$  = 30° and 60° for L-14,  $\theta$  = 30° for L-12, and  $\theta$  = 30° for

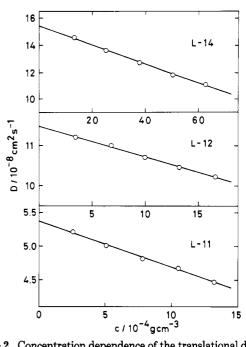


Figure 2. Concentration dependence of the translational diffusion coefficient D obtained for three PIP samples in 1,4-dioxane at 34.7 °C.

Table II Results of Dynamic Characteristics  $D_0$ ,  $R_{\rm H}$ ,  $k_{\rm D}$ , and  $\rho$  Obtained for Polyisoprenes in 1,4-Dioxane at 34.7 °C

polymer	$D_0$ , $10^{-8} \text{ cm}^2 \text{ s}^{-1}$	R <sub>H</sub> , 10 <sup>-6</sup> cm	$k_{ m D},~{ m cm^3~g^{-1}}$	ρ
L-14	15.4 <sub>2</sub>	1.435	-45.3	1.33
L-12	$11.4_{8}$	$1.92_{7}$	-66.2	1.31
L-11	$5.37_{4}$	$4.11_{7}$	-128	1.27

L-11, the quantity X ( $\equiv q^2R_{\rm G}^2$ ) was in the range from 0.03 to 0.24. Here q is the magnitude of the scattering vector. The translational diffusion coefficients at finite polymer concentration D(c) for the above three samples were estimated by fitting the  $A(\tau)$  data to a single exponential curve of the decay rate or the first cumulant  $\Gamma(c)$  ( $\equiv D(c)q^2$ ); i.e.,  $A(\tau) = \beta \exp(-2\Gamma(c)\tau) + 1 + \delta$ . Here  $\beta$  is a fitting parameter representing the amplitude and  $\delta$  is a fitting deviation of the base line from 1.000. The values of  $\delta$  were  $\pm 0.003$ . This confirmed the high reliability of present  $A(\tau)$  data and the analyses. Figure 2 shows the D(c) plotted against the concentration c. For each sample, the D(c)'s are well represented by the straight line, and the infinite dilution value  $D_0$  and the concentration coefficient  $k_{\rm D}$  were determined from

$$D(c) = D_0(1 + k_{\rm D}c) (2)$$

The results are summarized in Table II.

At  $\theta$  = 120° for L-12 and at  $\theta$  = 60°, 90°, and 120° for L-11, X ranged from 0.6 to 2.7. Hence, the  $A(\tau)$  data were analyzed by the histogram method<sup>10</sup> of bimodal distribution  $G(\Gamma)$ , of which the first (slow) mode was assigned to the translational diffusion motion. The effective decay rate (the first cumulant) at finite q and c,  $\Gamma_{\rm e}(q,c)$  was estimated by averaging  $\Gamma$  over the distribution  $G(\Gamma)$ . The amplitude of the translational diffusion mode relative to all molecular motions  $P_0/P$  was also evaluated from the fractional area of the first component in  $G(\Gamma)$ . Figure 3 shows concentration dependences of  $\Gamma_{\rm e}(q,c)/\sin^2{(\theta/2)}$  at constant q for solutions of L-11 and L-12. The data for given q are represented well by a straight line and give the value at infinite dilution,  $\Gamma_{e}(q,0)$ . These values are listed in Table III. The negative slopes in Figure 3 are characteristic of  $\Gamma_e$  in  $\theta$ -solvents.<sup>3</sup> Figure 4 shows concentration depen-

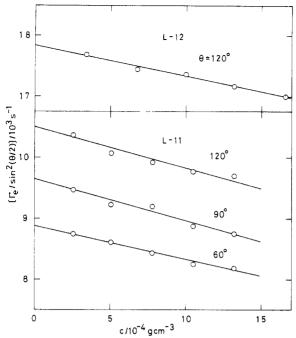


Figure 3. Linear extrapolation of the reduced effective decay rates  $\Gamma_{\rm e}(q,c)/\sin^2{(\theta/2)}$  for the solutions of L-12 at the scattering angle  $\theta=120^{\circ}$  and L-11 at  $\theta=60^{\circ}, 90^{\circ}$ , and  $120^{\circ}$ .

Table III
Results of Effective Decay Rate (First Cumulant) and Relative Amplitude of Translational Diffusion Motion at Infinite Dilution,  $\Gamma_{\rm e}(q,0)$  and  $(P_0/P)_{\rm c\to 0}$ , Obtained for Polyisoprenes in 1,4-Dioxane at 34.7 °C

polymer	angle, deg	X	$\Gamma_{\rm e}(q,0)/q^2,$ $10^{-8}~{ m s}^{-1}$	$(P_0/P)_{c\to 0}$
L-11	120	$2.74_{2}$	7.860	0.845
	90	$1.82_{8}^{-}$	$7.23_{4}$	0.912
	60	$0.914_{0}$	$6.64_{6}$	0.965
	30	$0.244_{9}$	$5.37_{6}$	
	$\theta \rightarrow 0$	0.0	$5.37_{6}$	
L-12	120	$0.636_{6}$	13.35	0.985
	30	0.0569	11.49	
	$\theta \rightarrow 0$	0.0	11.49	
L-14	60 30	$0.121_{9} \ 0.0327$	15.42	
	$\theta \rightarrow 0$	0.0	15.42	

dences of  $P_0/P$  at constant q for L-11 and L-12. The values of  $P_0/P$  at given q are nearly independent of c, as was the case for PS at the  $\theta$ -temperature, and give the infinite dilution values  $(P_0/P)_{c\to 0}$  within experimental error of 4%. The results are also summarized in Table III.

**Translational Diffusion Coefficient.** The molecular weight dependence of translational diffusion coefficients  $(D_0)$  listed in Table II can be given by

$$D_0 = 8.68 \times 10^{-5} M_{\rm w}^{-0.50 \pm 0.02} \tag{3}$$

The  $D_0$  values were converted to the equivalent hydrodynamic radius  $(R_{\rm H})$  by the relation

$$D_0 = k_{\rm B}T/6\pi\eta_0 R_{\rm H} \tag{4}$$

where  $k_{\rm B}$  is Boltzmann's constant and T is the absolute temperature. These values of  $R_{\rm H}$  versus  $M_{\rm w}$  are represented in Figure 1 by the filled circles. They are well represented by

$$R_{\rm H} = 2.57 \times 10^{-9} M_{\rm w}^{0.50 \pm 0.02} \text{ (cm)}$$
 (5)

The exponent of  $M_{\rm w}$ , 0.50±0.02, though its uncertainty is a little bit large due to three data points fitting, assures us that the present polymer–solvent system is in the  $\Theta$ -state. Since the  $R_{\rm G}$  data give the relation  $R_{\rm G} \propto M_{\rm w}^{0.50}$ , as

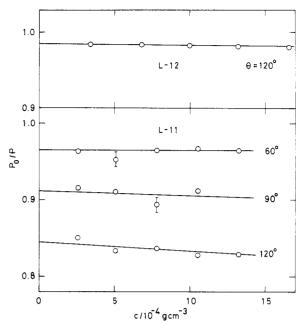


Figure 4. Linear extrapolation of the amplitude of the translational diffusion motion relative to the total motion  $P_0/P$  for the solutions of L-12 at  $\theta = 120^{\circ}$  and L-11 at  $\theta = 60^{\circ}$ ,  $90^{\circ}$ , and  $120^{\circ}$ .

already shown in the same figure by unfilled symbols, it is found that both  $R_{\rm H}$  and  $R_{\rm G}$  have the same  $M_{\rm w}$  dependence and  $R_{\rm H}$  is smaller than  $R_{\rm G}$  over the entire molecular weight region investigated.

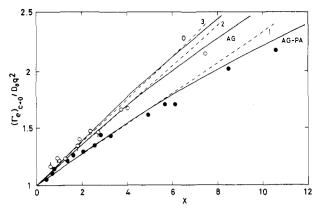
Defining a dimensionless parameter  $\rho$  by

$$\rho \equiv R_{\rm G}/R_{\rm H} \tag{6}$$

we can estimate its value as listed in Table II. The  $\rho$  was  $1.30 \pm 0.03$ , independent of the molecular weight. This value agrees, to within experimental error, with 1.27-1.283 for PS in  $\theta$ -solvents. It is thus found that the value is unaffected by the chain flexibility. However, this value of  $\rho$  is by about 13% smaller than 1.504 (= $\rho_K$ ) or 1.479 predicted by the classical theories of Kirkwood 11,12 or Zimm<sup>13</sup> with preaveraged and/or nonpreaveraged Oseen hydrodynamic interaction. We note also that the present value of 1.30 lies in the middle of  $1.40 \pm 0.01$ , <sup>14</sup> calculated by a Monte Carlo simulation, and 1.190,15 calculated from the renormalization-group techniques under non-PA scheme. Still another value of  $\rho$ , 1.285, has recently been obtained by Zimm<sup>16</sup> based on the simulation for Gaussian and cubic lattice chains. According to Fixman, 17 Zimm's algorithm gives a "lower-bound" value,  $\rho_{LB}$ , which is attained in a rigid body motion at sufficiently strong internal friction. Fixman<sup>17</sup> has revealed the following: (1) if the friction constants are independent of local chain structure, an "upper-bound" value,  $\rho_{\rm UB}$ , stays at about 1.38 (8% below  $\rho_{\rm K}$ ) irrespective of long Gaussian chains or lattice chains; (2) however, the  $\rho_{\rm UB}$  decreases down to near  $\rho_{\rm LB}$ when a very small amount of internal friction is introduced, which depends on the specified local nature of the chains.

In this connection, it may be interesting to note that in good solvent system,  $\rho_{\rm good}$  was about 1.5 for both PIP and PS and that the ratio to the  $\theta$ -value  $\rho_{\rm good}/\rho_{\theta}=1.15$  was close to 1.06 or 1.08, which was obtained by combining Kirkwood's<sup>11,12</sup> or Zimm's<sup>13</sup>  $\rho_{\theta}$  with  $\rho_{\rm good}$  for the Domb-Gillis-Wilmers segment distribution. 6,18

Internal Motions. Figure 5 shows, by the unfilled circles with vertical pip, the X dependence of the reduced value  $\Gamma_{\rm e}(q,0)/D_0q^2$  for the present data of PIP in 1,4-dioxane. The other circles are our previous data: the unfilled ones for PIP in cyclohexane (good solvent) at 25 °C<sup>6</sup> and



**Figure 5.** Plots of the reduced values of  $\Gamma_{\rm e}(q,0)/D_0q^2$  against  $X(=q^2R_{\rm G}^2)$ : (?) L-11 and (\$\delta\$) L-12, the present data for PIP in 1,4-dioxane at 34.7 °C; (O) PIP data in cyclohexane at 25 °C<sup>6</sup>; (•) PS data in *trans*-decalin at 20.4 °C.<sup>3</sup> The solid curves are the theoretical curves calculated for nondraining Gaussian chains: (AG-PA) Akcasu-Gural<sup>19-21</sup> curve with PA Oseen hydrodynamics; (AG) A-G curve with non-PA; (O) Oono<sup>22</sup> curve with non-PA. The broken lines represent the initial slopes for each curve: (1) 2/15; (2) 13/75; (3) 0.187.

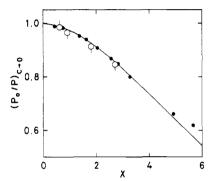


Figure 6. X dependence of the relative amplitude of translational diffusion motion  $(P_0/P)_{c\to 0}$ : ( $\circ$ ) L-11 and ( $\circ$ ) L-12 for the PIP data in 1,4-dioxane at 34.7 °C; ( $\bullet$ ) PS data in trans-decalin at 20.4 °C.<sup>3</sup> The solid curve represents the theoretical value for nondraining Gaussian chains.

the filled ones for PS in trans-decalin at θ-temperature.<sup>3</sup> The solid curves AG and O are the theoretical curves of Akcasu–Gurol (A–G)<sup>19–21</sup> and Oono,<sup>22</sup> respectively, for the nondraining Gaussian chains with non-PA Oseen hydrodynamics, and the curve AG–PA is the A–G curve with PA hydrodynamics. The broken lines 1, 2, and 3 represent the initial slopes, 2/15, 13/75, and 0.187, for curves AG–PA, AG, and O, respectively. The PIP data are located near curve AG and support non-PA hydrodynamics irrespective of the solvent power. This is different from the PS data; they are located near curve AG–PA. The difference might be attributed to the high chain flexibility of PIP chains.

Figure 6 shows the amplitude of the translational diffusion motion relative to the total motion,  $(P_0/P)_{c\to 0}$ , as a function of X. Here the unfilled circles represent the PIP data, the filled circles our previous data for PS at  $\theta$ -temperature,<sup>3</sup> and the solid curve the theoretical one for nondraining Gaussian chains.<sup>10</sup> The data fall well on the curve and reconfirm the adequacy of the nondraining model.

Intermediate-Scale Motions. In Figure 7, the reduced effective decay rate  $\Gamma_{\rm e}(q,0)/(q^3k_{\rm B}T/\eta_0)$  is plotted against  $X^{1/2}$  for PIP (unfilled circles) and for PS (filled circles). The solid curves AG-PA, AG, and O represent the theoretical curves with the same meanings as in Figure 5 and give the asymptotic values at the large region of  $X^{1/2}$ ; 0.053 (AG-PA), 0.0625 (AG), and ca. 0.027 (O), respectively. Since the PIP data do not extend to a wide range of  $X^{1/2}$ ,

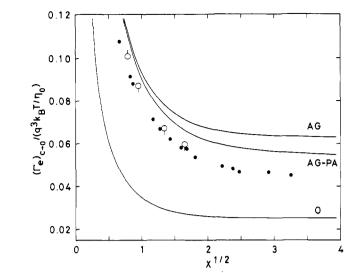


Figure 7. Plots of the reduced effective decay rate  $\Gamma_{\rm e}(q,0)/(q^3k_{\rm B}T/\eta_0)$  against  $X^{1/2}$ : ( $^{\circ}$ ) L-11 and ( $^{\circ}$ ) L-12 for the PIP data in 1,4-dioxane at 34.7  $^{\circ}$ C; ( $^{\bullet}$ ) PS data in trans-decalin at 20.4  $^{\circ}$ C. The solid curves are the theoretical curves calculated for nondraining Gaussian chains; (AG-PA) A-G curve<sup>19-21</sup> with PA; (AG) A-G with non-PA; (O) Oono<sup>22</sup> curve with non-PA.

they show no asymptotic feature as yet. However, they are located above and nearly parallel to the PS data within the range of  $X^{1/2}$  measured. This situation might give us an appropriate symptotic value 0.048 for PIP, while PS has given 0.045 at large  $X.^3$  Since the PIP data are well represented by non-PA calculation as mentioned in the previous section, we compare the result with the non-PA curve. The value 0.048 for PIP is however still smaller than the curve AG by 20%. At present there is no explanation as to why the difference is so large in the  $\theta$ -state. As referred in  $D_0$ , it may be expected that the internal friction would influence the  $\Gamma_{\rm e}(q,0)$  value. Stockmayer and Hammouda<sup>4</sup> have recently found some reduction of  $\Gamma_{\rm e}$  by advancing this scheme, but no reliable numerical estimate has been available.

Concentration Dependence of Translational Diffusion Coefficient. At the  $\Theta$ -temperature, the coefficient  $k_{\rm D}$  is related directly to the coefficient  $k_{\rm f}$  of the concentration dependence of the fraction coefficient as<sup>23,24</sup>

$$k_{\rm D} = -(k_{\rm f} + \bar{v}) \tag{7}$$

where  $\bar{v}$  is the partial specific volume of the polymer, and  $\bar{v}\approx 1.1~{\rm cm^3~g^{-1}}$  for PIP. For  $k_{\rm f}$ , several theories have been derived. They are summarized in the form

$$k_{\rm f} = BN_{\rm A}V_{\rm H}/M_{\rm w} = B'M_{\rm w}^{1/2}$$
 (8)

where  $N_{\rm A}$  is Avogadro's number and  $V_{\rm H}$  the hydrodynamic volume defined by  $V_{\rm H}=(4\pi/3)R_{\rm H}^3$ . In the large region of  $M_{\rm w}$ , the coefficient  $k_{\rm D}$  becomes proportional to  $M_{\rm w}^{1/2}$  because  $\bar{v}~(\approx 1.1)$  is negligibly small.<sup>24</sup> Theoretically the magnitude of B in eq 8 is 1.0 for the bead-spring model of Yamakawa<sup>23</sup> and Imai<sup>25</sup> (YI) and 2.23 for the soft-equivalent-sphere model of Pyun and Fixman<sup>26</sup> (PF) (Figure 8). Mulderije<sup>27</sup> has revised the PF value as 2.06 (M) and also shown, based on the study of Batchelor,<sup>28</sup> that  $B=1.60~({\rm MBa})$ . Akcasu<sup>29</sup> has proposed another value  $B=1.29~({\rm A})$  by using three different models for the intermolecular interactions. It is noted that the origin of B=1.0 by YI and the other values of B from other theories are different in the physical mechanisms they represent.<sup>36</sup>

The data of  $k_{\rm D}$ , listed in Table II, give the molecular weight dependence:

$$k_{\rm D} = -8.30 \times 10^{-2} M_{\rm w}^{0.50 \pm 0.05} \text{ (cm}^3 \text{ g}^{-1})$$
 (9)

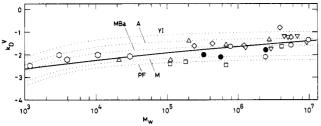


Figure 8. Plots of volume-fraction coefficient  $k_{\rm D}{}^{\rm V}$  against  $M_{\rm w}$  for the present data of PIP in 1,4-dioxane at 34.7 °C ( $\bullet$ ). The for the present data of PIP in 1,4-dioxane at 34.7  $^{\circ}$  ( ). The unfilled symbols are the data for PS in cyclohexane at 35  $^{\circ}$ C: ( $^{\circ}$ C: ( $^{\circ}$ King et al., $^{31}$  ( $^{\circ}$ ) Han; $^{32}$  ( $^{\circ}$ ) Jones and Caroline; $^{33}$  ( $^{\circ}$ ) Varma et al., $^{34}$  ( $^{\circ}$ ) Huber et al., $^{35}$  and in trans-decalin at 20.4  $^{\circ}$ C: ( $^{\circ}$ C: Tsunashima et al. $^{3}$  The dotted curves are the theoretical curves with the following  $^{\circ}$ B in eq 8: (YI)  $^{\circ}$ B = 1.0; $^{23,25}$  (A) 1.29; $^{29}$  (MBa) 1.60; $^{27,28}$  (M) 2.06; $^{27}$  (PF) 2.23. $^{26}$  The solid curve represents the best fit value for PS obtained by Tsunashima et al..30  $k_{\rm D} = -0.13 M_{\rm w}^{0.43} {\rm cm}^3 {\rm g}^{-1}$ .

The exponent 0.50 confirms eq 8, the theoretical prediction at 0-temperature. This is in contrast to the results for PS in  $\theta$ -solvents, where the best-fit exponent to all the data available was  $0.43 \pm 0.02.30$  For convenience' sake, the measured k<sub>D</sub> of mass fraction coefficient can be transformed into the volume fraction one,  $k_D^V$ , through a relation  $k_{\rm D}^{\rm V}=k_{\rm D}M_{\rm w}/N_{\rm A}V_{\rm H}$ . Figure 8 shows the  $M_{\rm w}$  dependence of the  $k_{\rm D}^{\rm V}$  for PIP (filled circles). Here  $V_{\rm H}$  was calculated from  $R_{\rm H}$  in Table II. The dotted curves YI, A, MBa, M, and PF represent the theoretical curves with B mentioned above. They show strong curvatures in the low  $M_{\rm w}$  region due to the large contribution of  $\bar{v}$  to  $k_{\rm D}^{\rm V}$ . The PIP data are located nearly on curve M (B = 2.06) rather than curve YI. This is in contrast to the results in good solvents where the Yamakawa theory was adequate. By unfilled symbols in the figure, we also show the molecular weight dependence of  $k_D^V$  values reported hitherto for PS in  $\theta$ -solvents (trans-decalin and cyclohexane). The values of  $V_{\rm H}$  were calculated from experimental values of  $R_{\rm H}$  reported in the references concerned. The correction of  $\bar{v}$  was also made to  $k_{\rm D}{}^{\rm V}$  in low molecular weight region. These PS data are located roughly between curves YI (B = 1.0) and PF (B = 2.23); in the region  $M_{\rm w} > 2 \times 10^5$ , they are closer to curve MBa (B = 1.60), while in the lower  $M_{\rm w}$ region,  $M_{\rm w} < 3 \times 10^4$ , they lie between curves A (B = 1.29) and M.<sup>37</sup> On the whole, all the data ranging from  $M_{\rm w} \approx$ 10<sup>3</sup> to 10<sup>7</sup> are satisfactorily represented by the solid curve which was transformed from the mass fraction  $k_{\rm D}$  versus M relation

$$k_{\rm D} = -0.13 M_{\rm w}^{0.43} \quad (\text{cm}^3 \text{ g}^{-1})$$
 (10)

with use of  $R_{\rm H}$  = 2.29 × 10<sup>-9</sup> $M_{\rm w}^{0.50}$  cm for PS in cyclohexane at 35 °C.<sup>1</sup> Equation 10 has been reported previously by us as the best fit curve for PS.30

## Conclusions

The PIP chains in 1,4-dioxane at 34.7 °C were found to be adequate to study dynamical properties of linear flexible chains in the unperturbed state. The dynamic properties were well described by the nondraining chain model with nonpreaveraged Oseen hydrodynamic interaction. However, there still remains some differences between experiments and theories in the magnitude of  $D_0$  (or  $\rho$ ) and

Registry No. PIP, 9003-31-0; 1,4-dioxane, 123-91-1.

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